

## 6 SCIENTIFIC HIGHLIGHT OF THE MONTH: Electronic Phenomena at Complex Oxide Interfaces: Insights from First Principles

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### Electronic Phenomena at Complex Oxide Interfaces: Insights from First Principles

Rossitza Pentcheva<sup>1</sup> and Warren E. Pickett<sup>2</sup>

<sup>1</sup> Department of Earth and Environmental Sciences, University of Munich,  
Theresienstr. 41, 80333 Munich, Germany

<sup>2</sup>Department of Physics, University of California Davis, Davis CA 95616, U.S.A.

#### Abstract

Oxide interfaces have attracted considerable attention in recent years due to the emerging novel behavior which does not exist in the corresponding bulk parent compounds. This opens possibilities for future applications in oxide based electronics and spintronics devices. Among the different materials combinations, heterostructures containing the two simple band insulators  $\text{LaAlO}_3$  and  $\text{SrTiO}_3$  have advanced to a model system exhibiting unanticipated properties ranging from conductivity, to magnetism, even to superconductivity. Electronic structure calculations have contributed significantly towards understanding these phenomena and we review here the progress achieved in the past years also showing some future directions and perspectives. A central issue in understanding the novel behavior in these oxide heterostructures is to discover the way (or ways) that these heterostructures deal with the polar discontinuity at the interface. Despite analogies to polar semiconductor interfaces, transition metal oxides offer much richer possibilities to compensate the valence mismatch, including *e.g.* an electronic reconstruction. Moreover, electronic correlations can lead to additional complex behavior like charge disproportionation and order, magnetism, and orbital order. We discuss in some detail the role of finite size effects in ultrathin polar films on a nonpolar substrate leading to another intriguing feature - the thickness dependent insulator-to-metal transition in thin  $\text{LaAlO}_3$  films on a  $\text{SrTiO}_3(001)$  substrate, driven by the impending polar catastrophe. The strong and uniform lattice polarization that emerges as a response to the potential buildup enables the system to remain insulating up to a few layers. However, beyond a critical thickness there is a crossover from an ionic relaxation to an electronic reconstruction. At this point two bands of electron and hole character, separated both in real and in reciprocal space, have been shifted sufficiently by the internal field in  $\text{LaAlO}_3$  to impose the closing of the band gap. We discuss briefly further parameters that allow one to manipulate this behavior *e.g.* via vacancies, adsorbates or an oxide capping layer.

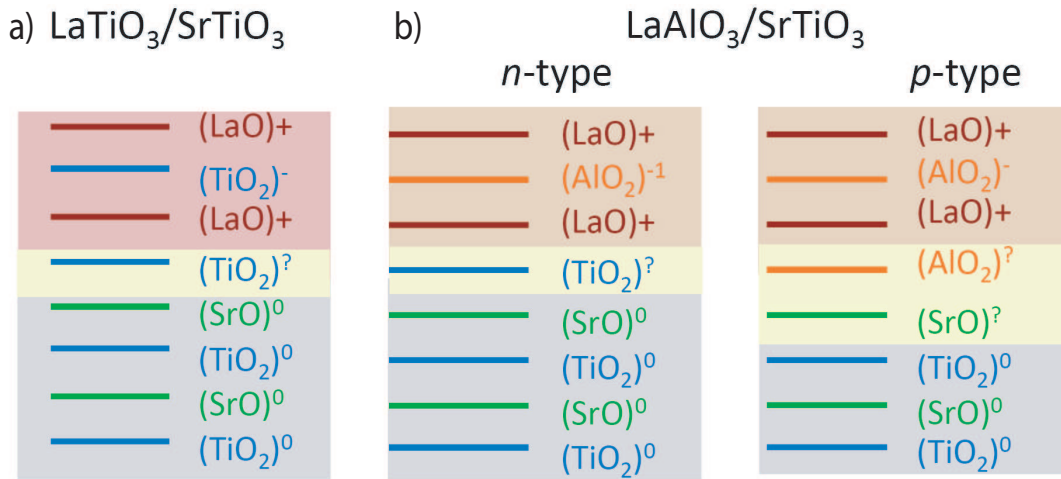


Figure 1: Schematic picture of the charge discontinuity at the a)  $\text{LaTiO}_3/\text{SrTiO}_3$ , as well as the b)  $n$ - and  $p$ -type interfaces in  $\text{LaAlO}_3/\text{SrTiO}_3$ . Due to mismatch of charges, the ions cannot maintain their formal valence at the interface.

## 1 Introduction to polar oxide surfaces and interfaces

As common as ionic insulators are – your table salt, for example – electronically they are very specific materials. In the band picture of electronic structure, in a conventional (band) insulator the Fermi level falls between two band complexes, and there are *precisely* enough electrons available to fill the lower set of (valence) bands and leave none in the upper set of (conduction) bands. In ionic oxides, it is common for the ions to be closed shell, and the ionic solid is insulating because the individual constituents are nondegenerate and stable. For such a conventional insulator to conduct, carriers must be coerced into otherwise filled or unfilled bands of states *e.g.* through doping.

A different type of oxide insulator arises when ions have partially filled shells. These transition metal compounds are known as Mott insulators, and fail to conduct because (in the classical simplest picture) the energy gain from hopping between the open-shell ions (roughly speaking, proportional to the bandwidth  $W$ ) is outweighed by the interaction energy cost of putting an extra electron on an ion (the Coulomb repulsion  $U$ , also known as the “Hubbard  $U$ ”). In practice, there are a number of energy scales and degrees of freedom that make the behavior much more complex and interesting. For these reasons, and because they give rise to the high temperature superconductors, these Mott insulators remain, after 50 years of study, a very active field of research.

Transition metal oxides exhibit both an impressive structural variety and a rich spectrum of functionalities such as high  $T_c$  superconductivity, magnetism, ferroelectricity and colossal magnetoresistance, among many others. In a heterostructure such properties can be combined, *e.g.* in the search for multiferroic materials (see for example  $\Psi_k$  Highlight 93 by Fechner *et al.*). However, perhaps a more compelling reason to study oxides is that it has become clear that novel electronic states can be realized at oxide interfaces that do not exist in the bulk phases.

Layer-by-layer growth allows synthesis of phases that are not thermodynamically stable. Recent developments of growth techniques like pulsed laser deposition (PLD) and molecular beam epitaxy (MBE) have enabled the synthesis of oxide superlattices with atomic precision [1,2]. These artificial “digital” materials are currently a source of excitement both from a fundamental point of view and for future technological applications in electronics and spintronics devices because of the novel functional properties that arise. Prominent examples are the two-dimensional electron gas measured at the interface between the Mott-insulator  $\text{LaTiO}_3$  (LTO) and the band insulator  $\text{SrTiO}_3$  (STO) [2], as well as between the two simple band insulators  $\text{LaAlO}_3$  (LAO) and STO [3]. Reports of superconductivity [4] and magnetism [5] in the latter system have fueled research both on the theoretical and experimental side. Due to the emerging new functionalities and the underlying fundamental questions, *Science* magazine selected oxide interfaces as one out of ten “runners-up” in the breakthroughs of 2007 [6]. This area of research was also featured in an editors article in *Physics Today* [7].

As we will relate in this article, symmetry breaking and charge neutrality violation at the interface play a central role in the emergence of unexpected behavior. Analogous to oxide surfaces [8–10] the question of polarity arises also at oxide interfaces. In the perovskite structure the ionic charge is modulated along the [001] crystallographic direction, e.g. in  $\text{LaTiO}_3$  positively charged  $(\text{La}^{3+}\text{O}^{2-})^+$ -layers alternate with negatively charged  $(\text{Ti}^{3+}\text{O}_2^-)^-$ -layers, while  $\text{SrTiO}_3$  consists of formally neutral  $(\text{Sr}^{2+}\text{O}^{2-})^0$ - and  $(\text{Ti}^{4+}\text{O}_2^-)^0$ -layers. As shown in Fig. 1 a valence discontinuity arises at the (001)-interface (IF) between the polar LTO and the nonpolar STO, i.e. there is  $\frac{1}{2}$  electron per IF cell in excess for the formal charge states of STO to be maintained, or  $\frac{1}{2}$  too little for LTO. This excess of charge corresponds to carrier densities around  $3.5 \times 10^{14}$ . The situation is similar in LAO/STO: at the *n*-type IF there is half an electron too much to keep the formal charges, while with a SrO-AlO<sub>2</sub> stacking (*p*-type) there is an extra  $\frac{1}{2}$  hole.

During the film growth process of polar materials it is expected that the dipoles lead to a shift of the potential which increases proportional to the number of overlayers (i.e. a constant electric field). [11] This impending “polar catastrophe” has to be accommodated in some way. At first glance polar oxide interfaces bear similarities to polar semiconductor heterostructures. For the latter, compensation is often achieved through the so-called atomic reconstruction, where the surface/interface chemical composition is strongly altered via ordering of defects or roughening. On the other hand, at oxide interfaces an electronic reconstruction involving electron transfer into unoccupied bands can take place. Taking into account the correlated nature of the 3*d*-electrons and the possibility of multiple valence states in transition metal ions, more complex compensation mechanisms can arise leading to the stabilization of novel electronic phases.

*Ab initio* calculations play a key role in understanding the physics at oxide interfaces, but we note also that the structural complexity, the large system sizes and, last but not least, the treatment of electronic correlations pose high demands on the theoretical description. Rather than providing a full review of all theoretical work done so far, we have selected several cases that exemplify the insight that can be obtained from density functional theory (DFT) calculations, focusing on interfaces between polar and nonpolar materials. Most of the results presented here are obtained using the full-potential linearized augmented plane waves method as implemented in the WIEN2k code [13] and the generalized gradient approximation [14] to the exchange correlation potential also including correlation effects within the LDA/GGA+*U* method [12]

(for more details the reader is referred to the original papers). Specifically, we will compare the compensations mechanisms that arise in heterostructures of the Mott insulator LTO and the band insulator STO to those comprised of the conventional ionic insulators LAO and STO. The latter is chosen both because it shows a striking variety of properties making it by far the most studied system, and also because the remarkably intricate behavior of these rather simple materials ought to be understood before one deals with the additional complexity arising from the “Mott physics” in open shell transition metal oxides. In Section 2 we address the electronic properties of infinitely extended superlattices of LTO/STO and compare them to those at the isolated  $n$ - and  $p$ -type LAO/STO interfaces (Section 3.1 and Section 3.2, respectively). The latter are contrasted in Section 3.3 to the behavior of thin LAO films on a STO(001) substrate, where we explore finite size effects and the origin of the intriguing thickness-dependent insulator-to-metal transition. In Section 4 we summarize the current state of understanding of these materials and mention some future perspectives.

## 2 Compensation mechanisms at the $\text{LaTiO}_3/\text{SrTiO}_3$ interface

$\text{SrTiO}_3$  is a band insulator with a band gap of 3.2 eV. Due to the well known problem of the local density approximation (LDA) or GGA to underestimate the band gap, the GGA band gap separating occupied O  $2p$  states from unoccupied Ti  $3d$  states is 2.0 eV. In contrast, in  $\text{LaTiO}_3$  the Ti  $3d$  band is singly occupied and a strong intra-atomic Coulomb repulsion on the Ti ion leads to Mott insulating behavior.  $\text{LaTiO}_3$  is one of the most studied correlated insulators. In bulk form its perovskite structure is strongly distorted, which narrows the  $3d$  bands and thereby contributes to the Mott insulating character. The connection between the Jahn-Teller distortion and strong interaction effects in this compound is still a subject of intense research. [15]

Experiments indicate that LTO grows coherently on STO. The lattice mismatch between LTO ( $a = 3.97\text{\AA}$ ) and STO ( $a = 3.905\text{\AA}$ ) is relatively small (2%) and produces a tetragonal distortion which breaks the  $t_{2g}$  degeneracy when LTO is incorporated into superlattices grown on STO substrates. The effect of the pseudocubic structure and the tetragonal distortion is one of the relevant issues that will be discussed in the following.

“Interdiffusion layers” of LTO/STO with sheet carrier densities in the range  $10^{13} - 10^{15} \text{ cm}^{-2}$  were grown in 1996 by Yoshida and collaborators [16]. In 2002 Ohtomo *et al.* [2] reported abrupt IFs involving LTO and STO demonstrating atomic control of the number of LTO layers within the STO host during the PLD process. Annular dark field transmission electron microscopy (TEM) images indicated atomically sharp interfaces. The observed conductivity at the interface between two insulators opened up the study of polar IFs with one strongly correlated component. Electron energy loss spectra (EELS) indicated a mixed  $\text{Ti}^{3+}$ ,  $\text{Ti}^{4+}$  signal close to the interface with a decay length into the STO host of the order of 1 nm, which stimulated and focused some of the early theoretical work. Subsequent studies [17–20] reported more characteristics, including nanostructures with high mobility [19] as well as samples with poor conductivity. [20] Photoemission studies of buried LTO/STO IFs found a sharp Fermi cutoff (itinerant states), becoming sharper after  $\text{La} \leftrightarrow \text{Sr}$  interdiffusion due to annealing [21].

## 2.1 Model Approaches

Before turning to the first principles studies of this system we review briefly the results from model Hamiltonian approaches. The theoretical study of this Mott insulator-band insulator interface was initiated by Okamoto and Millis, using single and then multiple band Hubbard models and a statically screened Coulomb interaction  $e^2/|R-R'|$  interaction [22]. This approach results in a complex phase diagram with ferromagnetic, antiferromagnetic, and nonmagnetic solutions, as well as orbitally-ordered phases in certain regimes. Employing a similar approach but an exact diagonalization for a one-dimensional chain and two-leg ladders, Kancharla and Dagotto [23] obtained that the charge disturbance extended over nine or more atomic layers away from the interface even for large interaction strength. Lee and MacDonald considered [24] again a Hubbard model with similar interactions, with new features including a Thomas-Fermi (TF) treatment of the system, and consideration of a finite system (thin film). The TF solution provided a guideline in analytic form for the minimum number of layers required to drive the electronic reconstruction at the IF. More recently, Sigrist and coworkers [25] have addressed similar model Hamiltonians using auxiliary boson (slave boson) mean field theory. For (1) a correlated slab (variable interaction strength) embedded within a band insulating material ("STO"), and (2) multilayers they obtained a metallic (though highly renormalized) quasiparticle behavior even in the strongly interaction limit: a 2D electron gas.

## 2.2 DFT studies of electronic and orbital reconstruction

The odd number of electrons near the interface will give in the local density approximation (LDA) at least one partially filled band, *i.e.* a metallic IF. This metallicity is likely to persist when spin polarization (LSDA) is included, though insulating solutions are in principle possible in LSDA. The early DFT-based studies of the LTO/STO IF adopted the LSDA (or GGA) description, necessarily obtaining metallic IFs. [26,27] One emphasis was on the degree of confinement of the conducting layer to the IF region, which was attributed to a wedge shaped potential due to the incorporated LaO layer [26]. Both of these studies found a decay length of roughly three unit cells: the charge is spread over several  $\text{TiO}_2$  layers away from the interface with intermediate valent  $\text{Ti}^{3+\delta}$  ions.

To model superlattices containing a Mott and a band insulator, we have adopted the LDA+ $U$  [12] (GGA+ $U$ ) method as a standard approach to describe the Mott insulating nature of LTO. A variety of heterostructures were considered, where the number of LTO ( $n$ ) and STO ( $m$ ) layers was varied  $1 \leq n, m \leq 9$ . In the following we denote these superlattices by  $\text{LTO}_n/\text{STO}_m$ . To describe the antiferromagnetic (AFM) G-type coupling of LTO (rocksalt arrangement of the Ti-spins), but most importantly to allow more complex electronic reconstructions and magnetic order, the lateral cell was enlarged to  $c(2 \times 2)$  or  $p(2 \times 2)$ .

The initial question that arises is the appropriate value of the on-site repulsion parameter (Hubbard)  $U$  to choose. Calculations for an undistorted LTO crystal in a tetragonal setup (to model the magnetic coupling) show that a value of  $U = 8$  eV, and intra-atomic Hund's  $J = 1$  eV is needed to obtain an AFM-G type insulator. This value is somewhat higher than the one generally used for titanates with a distorted perovskite structure [31].

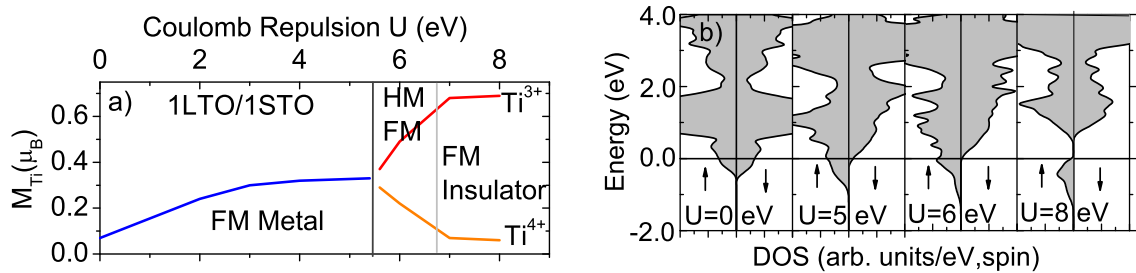


Figure 2: a) Evolution of the magnetic moment of Ti in a  $\text{LTO}_1/\text{STO}_1$  superlattice (SL) with a  $c(2 \times 2)$  lateral periodicity as a function of the Hubbard  $U$ -parameter. b) Density of states (DOS) (arrows denote the majority and minority DOS) (1,1)-SL for different  $U$  values. A charge disproportionation occurs beyond  $U \approx 5.5$  eV. HM FM denotes the region where the system shows half metallic ferromagnetic behavior, before a Mott-Hubbard band gap forms at around  $U \approx 6.5$  eV. [28]

For a  $\text{LTO}_1/\text{STO}_1$  superlattice (which in fact corresponds to one type of double perovskite compound), we have investigated how the value of  $U$  influences the behavior of the Ti ion. As shown in Fig. 2 for  $U=0$  a small moment of  $\approx 0.07\mu_B$  moment arises on the Ti ions. With increasing  $U$  up to 5 eV the magnetic moments of the two equivalent Ti-ions at the interface increase and saturate at  $0.33\mu_B$ . In this region the system is a ferromagnetic (FM) metal. However, beyond this value charge disproportionation emerges, making the system a ferromagnetic half-metal for  $5 < U < 7$  eV, before a band gap opens up for  $U > 7$  eV separating the lower Hubbard band from the unoccupied  $3d$  states. In the strong interaction regime a layer of  $\text{Ti}^{3+}$  and  $\text{Ti}^{4+}$  ions ordered in a checkerboard arrangement emerges at the interface. As shown in Fig. 3 the extra electron at the  $\text{Ti}^{3+}$  sites occupies the  $d_{xy}$ -orbital. This is not true orbital ordering because the Ti ion lies at the IF and the lowered symmetry breaks the degeneracy of the  $t_{2g}$  orbitals, with  $d_{xy}$  lying lowest. The local  $\text{Ti}^{3+}$  moment, reduced by mixing with oxygen as is common in oxides, is  $0.72\mu_B$ ; the total moment per IF cell including the induced moment on the O ion is enforced by the FM insulating state to be  $1\mu_B$ . Finally, an antiferromagnetic coupling between  $\text{Ti}^{3+}$  within the interface layer becomes energetically favored [28].

This  $\text{LTO}_1/\text{STO}_1$  heterostructure is however more a synthetic compound than a periodic array of interfaces. To determine the compensation mechanism and relaxation length towards bulk behavior at an isolated interface, we have studied more extended superlattices. The change in the electronic structure across a  $\text{LTO}_1/\text{STO}_5$  multilayer with *ideal positions* of the atoms is displayed in Fig. 4a. Within GGA+ $U$ , the charge mismatch is accommodated essentially entirely in the IF layer which contains charge ordered  $\text{Ti}^{4+}$  and  $\text{Ti}^{3+}$ . The  $\text{Ti}^{4+}$  ion in the next layer on the STO side has a projected density of states that is nearly identical to that of bulk STO. Analogously,  $\text{Ti}^{3+}$  ions one cell away from the IF in a superlattice with a thicker LTO part ( $\text{LTO}_5/\text{STO}_5$  - not shown here) is similar to that of bulk LTO. Small differences between  $\text{Ti}^{4+}$  and  $\text{Ti}^{3+}$  ions in the IF layer and their counterparts in the bulk can be attributed to the different environment.

Hamann *et al.* [27] and Okamoto *et al.* [29] pointed out the importance of the structural relaxations on the electronic properties. This strong electron-lattice coupling has become essential to understand the behavior near IFs involving polar discontinuities. GGA [27] and LDA+ $U$  [29] calculations within a  $p(1 \times 1)$  unit cell predict a strong ferroelectric distortion of  $0.15 \text{ \AA}$  in the



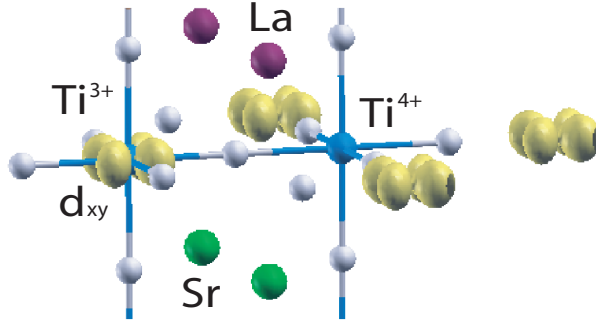


Figure 3: Spatial distribution of the electron density integrated between  $-2$  eV and  $E_F$  showing the charge and orbitally ordered state at the LTO/STO interface. For  $U = 8$  eV  $\text{Ti}^{3+}$  and  $\text{Ti}^{4+}$  order in a checkerboard arrangement with an occupied  $d_{xy}$ -orbital at the  $\text{Ti}^{3+}$ -sites, and no charge at the  $\text{Ti}^{4+}$  sites.

interface  $\text{TiO}_2$ -layer leaving the Ti-Ti distance across the LaO layer larger than the Ti-Ti distances within the STO slab. The lattice distortion quickly decays away from the IF into the STO host. As shown in Fig. 4b these lattice relaxations invoke small but nonetheless important band shifts compared to the ideal structure: the occupied Ti  $d_{xy}$  state (the lower Hubbard band) rises by 0.3-0.4 eV, closing the very small gap and leading to partially filled bands and conducting behavior. A small concentration of holes are introduced into the  $d_{xy}$  band, with the compensating electrons going into deeper layers in the STO slab in Ti-orbitals of  $d_{xz}$ ,  $d_{yz}$  character. This orbital occupation is sustained even at the GGA level [30]. Within GGA+ $U$  the IF layer of Ti ions remains charge-ordered and magnetically ordered, in spite of the  $\sim 30\%$  occupation of holes in the band and a reduction of the magnetic moment at  $\text{Ti}^{3+}$  to  $0.49 \mu_B$ . Overall, the lattice polarization obtained within GGA redistributes and smooths the charge profile, resulting in a larger relaxation length towards bulk behavior in the STO host [27, 29].

On the other hand, a structural relaxation within GGA+ $U$  taking into account a larger  $c(2 \times 2)$  lateral periodicity results in quite a different electronic behavior. While the vertical relaxations are slightly weaker than within GGA, a lateral relaxation of the oxygen ions away from the  $\text{Ti}^{3+}$  sites (breathing mode) leads to a further stabilization of the charge and orbitally ordered state. Moreover, the splitting between the occupied Ti  $d_{xy}$  orbital and the rest of the  $t_{2g}$  states is enhanced leading to a larger band gap as displayed in Fig. 4c.

This charge and orbitally ordered phase at the LTO/STO interface results from the interplay of electronic correlations and additional degrees of freedom and is an example how these can lead to unexpected compensation mechanisms of the interface polarity involving novel electronic states.

Since x-ray diffraction experiments [18] indicate only a tetragonal (and not orthorhombic) distortion for the epitaxial LTO layers in these heterostructures, an important issue is whether LTO can preserve its insulating character without the  $\text{GdFeO}_3$ -type distortion of the bulk compound. The question of the (non)conducting character of pseudocubic LTO has been addressed by Ishida and Liebsch. [32] using a LDA+DMFT (dynamical mean field theory) method includ-

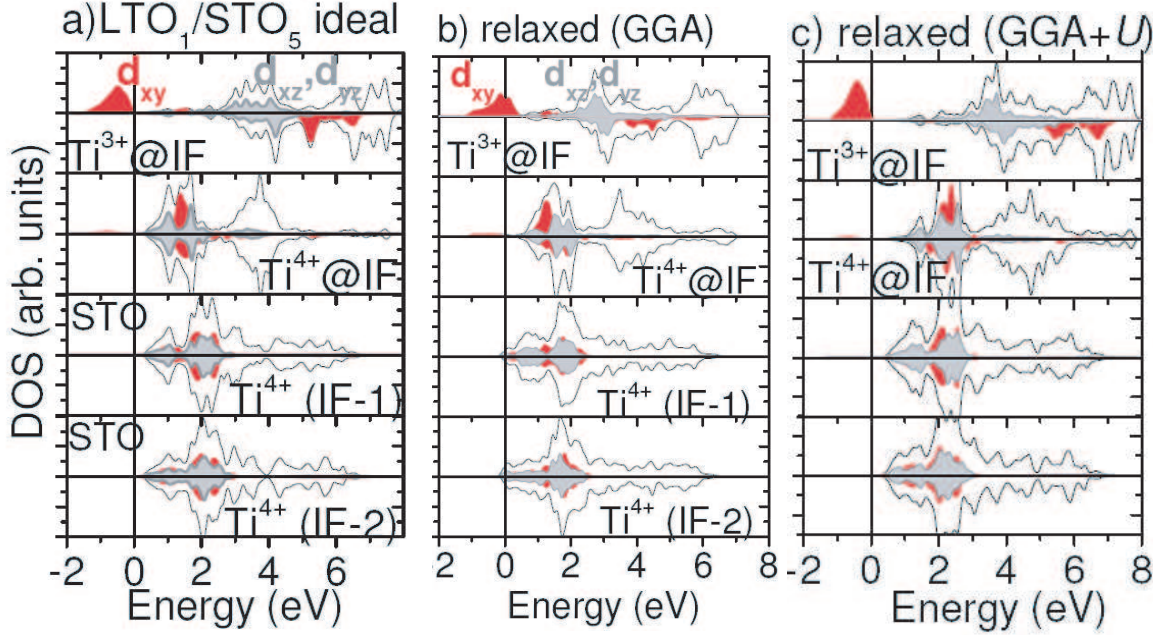


Figure 4: Layer-resolved projected DOS of the Ti 3d-states in the LTO<sub>1</sub>/STO<sub>5</sub>-heterostructure with ideal (a) and relaxed positions of the ions (b) within GGA and (c) within GGA+ $U$ . For the structure related within GGA the excess charge leaks into the STO host [28], while relaxation within GGA+ $U$  stabilizes further the charge and orbitally ordered state at the interface.

ing the Ti 3d states and treating the on-site interaction with exact diagonalization techniques. For tetragonal LTO appropriate to growth on STO, they obtained a metal-insulator transition in LTO at  $U = 6$  eV ( $J = 0.65$  eV). This critical value of  $U$  is not much different than what we obtained from GGA+ $U$ . However, assuming that  $U = 5$  eV is more appropriate for Ti, the authors conclude that tetragonal LTO itself is metallic, and that this accounts for the conducting LTO/STO multilayers that are observed experimentally. Using this value of  $U$  and treating (LTO)<sub>3</sub>/(STO)<sub>4</sub> multilayers, they find that some of the Ti charge in LTO is transferred into the STO layers. Since the Fermi level of LTO must lie within the STO gap, this leaking of charge into STO would be like the “metal-induced gap states” that are well studied in conventional metal-semiconductor IFs.

### 2.3 Compensation through La,Sr intermixing

Besides the possibility of an electronic reconstruction, we have also considered an atomic reconstruction through an intermixed (La,Sr) layer. The projected DOS of a superlattice containing two unit cells of LTO and STO with one mixed La, Sr layer at the interface is shown in Fig. 5. While Ti ions on the LTO side of the interface behave nearly as in the Mott insulating bulk material, the Fermi level crosses the  $d_{xy}$  band of Ti<sup>3+</sup> next to the interface. The  $t_{2g}$  bands of Ti<sup>4+</sup> on the STO side have also a small occupation, leaving the system conducting. This is possibly related to the fact that solid solutions of LTO and STO (LSTO) are conducting even for small doping concentrations of Sr [33,34] in LTO, or La in STO.



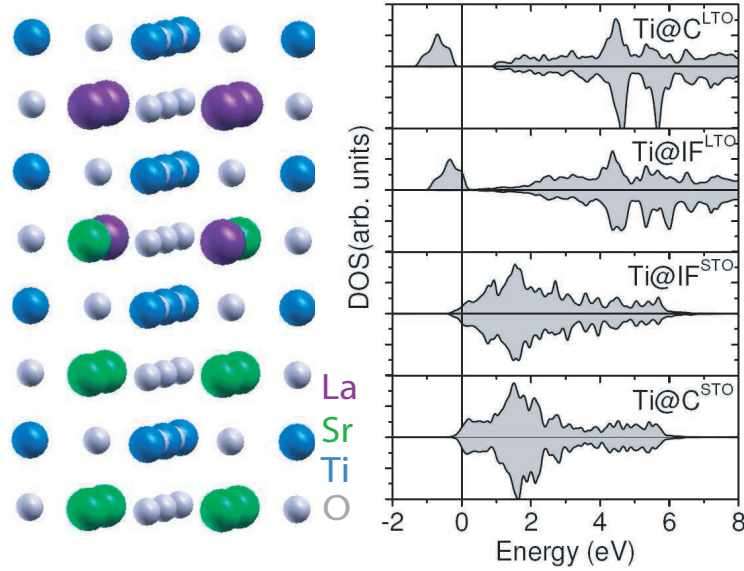


Figure 5: Layer-resolved projected DOS of the Ti  $3d$ -states in the  $\text{LTO}_2/\text{STO}_2$ -heterostructure with an intermixed La,Sr-layer. In the central Ti layer of the LTO slab, Mott insulating behavior is retained. The LTO side of the interface can be considered as a slightly (hole) doped Mott insulator, and compensating electrons must lie in the conduction bands on the STO side of the interface.

The implications of strong electronic correlations at the LTO/STO IF have certainly not been completely resolved. It is also important that more widely spaced IFs be studied to corroborate the results on the isolated IF. In the meantime, however, the limelight and the effort have both been concentrated on the LAO/STO system, which we will discuss in the next Section.

### 3 Compensation mechanisms in the $\text{LaAlO}_3/\text{SrTiO}_3$ system

At an LAO/STO interface both the A and the B cations change across the interface, leading to two distinct types of interfaces: the electron doped  $n$ -type interface with a LaO-layer next to a  $\text{TiO}_2$  layer and the hole doped  $p$ -type interface where a SrO-layer lies next to a  $\text{AlO}_2$ -layer (see Fig. 1). The interest in this system was triggered by experimental findings that the  $n$ -type interface between these two band insulators is conducting, while the  $p$ -type interface was reported to be insulating [3]. The high electron mobility ( $10^5 \text{ cm}^2/\text{Vs}$ ) and carrier density<sup>1</sup> ( $\sim 10^{17} \text{ cm}^{-2}$ ) initially reported for the  $n$ -type interface suggested possible applications in oxide based electronic devices and invoked a surge in both theoretical and experimental studies. In later studies, however, it became clear that growth conditions during the PLD process play a decisive role and that the unusually high carrier density is rather related to the formation of oxygen vacancies during the deposition process [11, 35–38]. This *extrinsic* conductivity has a predominantly 3D character [39]. Increasing the oxygen partial pressure during growth or subsequent annealing in an oxygen atmosphere leads to an increase in sheet resistance by several orders of magnitude. In fact the three functional properties observed so far can be related to three different regions of

<sup>1</sup>Note that the intrinsic carrier density scale of one-half carrier per interface cell equals to  $3 \times 10^{14} \text{ cm}^{-2}$ .

oxygen pressure [40]: (3D) conductivity at  $p_{\text{O}_2} \sim 10^{-6}$  mbar, superconductivity at  $p_{\text{O}_2} \sim 10^{-4}$  mbar [4], while magnetic effects [5] are observed at  $p_{\text{O}_2} \sim 10^{-3}$  mbar.

Many of the theoretical studies so far have focused on the origin and type of carriers at the interface leading to conductivity. The formal charge mismatch at the polar interface means that there will be too many (*n*-type interface) or too few (*p*-type interface) electrons to satisfy the formal charges, so there must be potential carriers in the interface regions. As just discussed, the initially measured conductivity is extrinsic in nature. Films grown at “high” oxygen pressures, where the effect of oxygen defects is minimized, are (nearly) insulating at low temperature. The fact that carriers seem to become localized at low temperature is a more challenging result to explain than if they were simply free and conducting. We restrict our discussion to this regime of defect-free heterostructures where the influence of oxygen vacancies can be neglected.

### 3.1 The *n*-type LaAlO<sub>3</sub>/SrTiO<sub>3</sub> interface

In order to model the *n*-type interface most studies have adopted multilayers containing two inversion symmetric *n*-type interfaces to avoid the formation of a net dipole in the the slab with its resulting spurious electric field. From electron counting one expects that the odd number of electrons per interface cell must give a metallic result within LDA. This was confirmed for both *n*-type and *p*-type IFs [41–43]. Gemming and Seifert [41] found the “excess” charge for either *n*- or *p*-type interfaces to be rather strongly localized to within a couple of layers of the interface and that the metallic state can be canceled by adding a background charge. The dielectric properties determined from linear response theory show a strong dependence not only on strain but also on the local interface chemistry. Popovic *et al* [44] investigated more extended superlattices with the *n*-type interface and, also after relaxation, concluded that the interfacial charge extended several layers away from the interface layer. This study noted multi-subband occupation, with some electron remaining localized at the interface while other bands contained more delocalized electrons. This aspect will be discussed in more detail below.

Because the LaO-TiO<sub>2</sub> layers at the *n*-type interface constitute the building block of the Mott insulator LTO, we have considered the role of correlation effects also in this case. Indeed, the resulting compensation mechanism is very similar to the one in LTO/STO superlattices with a charge disproportionation into a charge (CO) and orbitally ordered (OO) state with Ti<sup>3+</sup> and Ti<sup>4+</sup> ordered in a checkerboard arrangement [42].

The role of lattice relaxations has been investigated considering more isolated interfaces in a LAO<sub>4.5</sub>/STO<sub>5.5</sub> superlattice (with  $a_{\parallel} = a_{\text{STO}} = 3.91\text{\AA}$ ) shown in Fig. 6 [45]. The lattice relaxation was performed separately within GGA and GGA+*U*. The main characteristic, common to both, is a strong polarization in the layers close to the interface, predominantly in the STO part of the heterostructure, whereas in the LAO layer next to the IF both cations and anions shift by similar amounts. Analogous to the LTO/STO interface (see previous Section) a strong buckling in the interface TiO<sub>2</sub> layer by 0.17 Å (GGA) and 0.12 Å (GGA+*U*) is found. The precise value of lattice polarization at the interface varies slightly with the separation between the interfaces and the lateral lattice parameter [41, 43, 47].

While the atomic displacements within both approaches show similar trends, they have some-

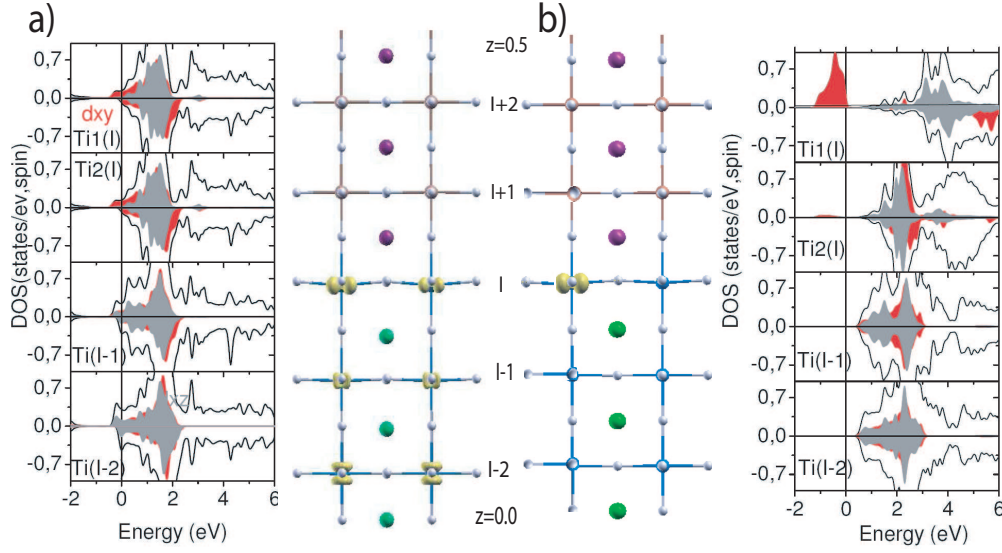


Figure 6: Layer resolved DOS obtained within GGA+ $U$  showing the Ti 3d bands and side views of the LAO<sub>4.5</sub>/STO<sub>5.5</sub> superlattice, relaxed within a) GGA and b) GGA+ $U$ . The side views display also the spatial distribution of the occupied 3d-orbital at the Ti-sites. Structural relaxation within GGA+ $U$  leads to two distinct Ti sites at the interface: Ti<sup>3+</sup> and Ti<sup>4+</sup>, while the GGA-geometry results in two identical Ti ions in the IF layer and finite occupation of Ti 3d states in deeper layers [45].

what higher absolute values within GGA. Still, subtle differences (e.g. a small lateral shift of the oxygens away from the Ti<sup>3+</sup>-ions) result in a completely different electronic behavior for the GGA+ $U$  and the GGA geometries. For the former the charge and orbitally ordered state is further stabilized and the charge is strongly confined to the interface layer (see Fig. 6b) [45]. Zhong and Kelly [49] have addressed further symmetry lowering due to rotations/tilting of the octahedra that narrow the Ti 3d band and found that these are energetically favorable even within LDA. Including correlation effects with the LDA+ $U$  method, they obtain a similar charge disproportionation, orbital reconstruction and AFM coupling of the spins in the strong interaction limit.

In contrast, for the GGA geometry the excess charge is redistributed over the STO part of the LAO<sub>4.5</sub>/STO<sub>5.5</sub> heterostructure (see Fig. 6a). While CO is nearly suppressed, there is a residual orbital ordering with an occupation of the  $d_{xy}$  orbital of Ti in the interface layer, while in more distant layers the  $d_{xz}$ ,  $d_{yz}$  orbitals are occupied. Analyzing the band structure, Popovic, Satpathy, and Martin found [44] that the latter bands have a very small dispersion and lie a bit higher than the bottom of the dispersive  $d_{xy}$  band (at  $\vec{k}=0$ ). The authors proposed that only the latter contributes to the transport properties of the system. This gives a possible explanation that the measured carrier densities are one order of magnitude lower than the expected  $3.5 \times 10^{14} \text{ cm}^{-2}$ .

Still the CO/OO solution corresponds to the ground state (favored by 0.45 eV). For the samples grown at high pressures the sheet resistance is seven orders of magnitude higher and shows an upturn at low temperatures which is consistent with CO or polaronic behavior. Electron delocalization at higher temperatures may lead to the behavior described in Fig. 6a.

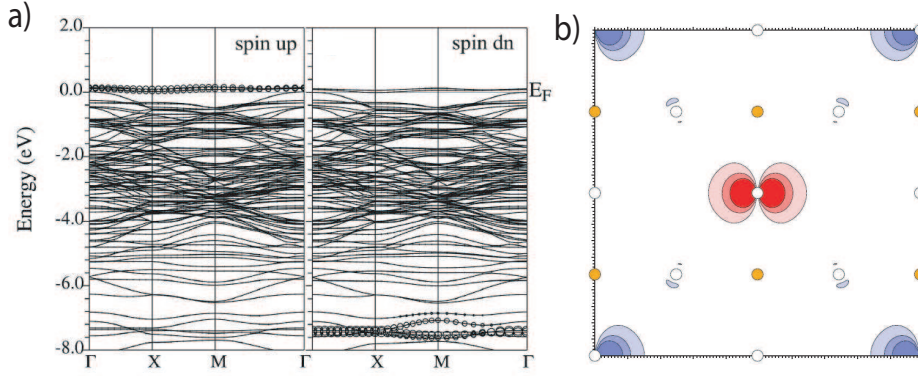


Figure 7:  $O\pi$ -holes at the  $p$ -type LAO/STO interface in a  $p(2 \times 2)$ -cell within GGA+ $U$ : (a) band structure, showing the strongly localized upper Hubbard band at the Fermi level and (b) spatial distribution of the antiferromagnetically coupled holes in the  $AlO_2$ -IF [42].

Several studies have addressed the band offsets at the  $n$ -type LAO/STO interface. Depending on the applied method: the reference potential method [63], the  $O1s$  core levels [44,45], the local density of states or the macroscopic averaging technique [46] there are notable differences (e.g. the calculated valence band offset varies between 0.1-0.9eV). In general, the STO band gap lies completely within the LAO gap, implying that charge carriers of either sign (electrons or holes) will go into the STO side of the interface.

To determine the confinement of the electron gas at the interface, Janicka *et al.* [50] have considered superlattices containing 23 MLs of STO and 1-5 layers of LAO. These GGA calculations determine a relaxation length of  $\sim 1$  nm. Using the  $O2s$  states to probe the band bending and the calculated band gap of bulk STO, these authors conclude that electrons 5 ML away from the interface occupy a classically forbidden region, forming so called metal-induced gap states.

### 3.2 The $p$ -type $LaAlO_3/SrTiO_3$ Interface

The  $p$ -type LAO/STO interface which was found to be insulating despite the charge mismatch has been less studied. The initial reports of Ohtomo and Hwang [3] suggested that the interface is structurally perfect *i.e.* without appreciable defects. For such an interface LDA/GGA gives a metallic solution with the Fermi level crossing the  $O2p$  band [42,43]. Since the occupied Sr and Al states lie well below the Fermi level, the only possibility to obtain insulating behavior (assuming a defect-free heterostructure) is to consider correlation effects at the  $O2p$  orbitals. Applying a Hubbard repulsion  $U$  on the  $O2p$  states with a single hole present, amounts to a lifting of the orbital degeneracy of the  $O2p$ -band. Considering the charges and geometry of Al and O in the  $AlO_2$  layers, it is likely that the holes will go into  $\pi$ -bonds. Indeed the GGA+ $U$  treatment results in a localization of a significant part of the hole on a central oxygen with some contribution of the nearest neighbors, while the next nearest neighbors are not affected (see Fig. 7b) and have a fully occupied  $O2p$  band. The holes are spin-polarized and the degree of localization of charge is enhanced for antiferromagnetic coupling. However, as shown in Fig. 7a, the upper Hubbard band is pinned at the Fermi level with some admixing of O in the next SrO layer. These calculations [42] were performed for superlattices with ideal positions of the atoms

where the two inversion symmetric interfaces are rather close. Including lattice relaxations and a better separation between the interfaces is likely to lead to an insulating polaronic solution.

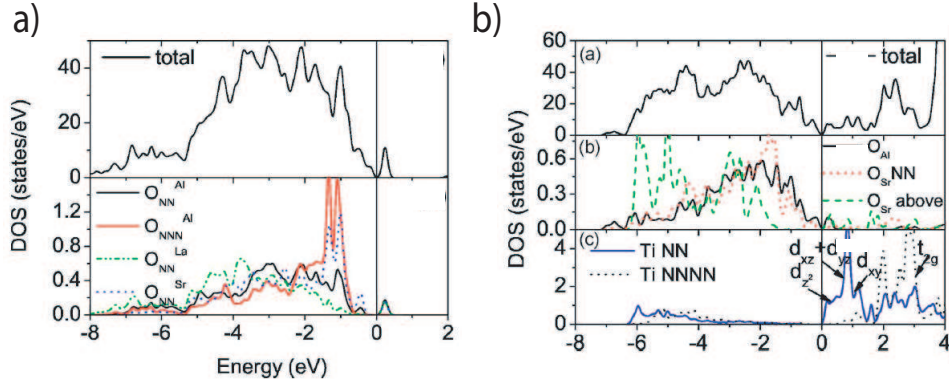


Figure 8: DOS of the  $p$ -type LAO/STO IF with an oxygen vacancy in the a)  $\text{AlO}_2$ -layer and b) SrO-layer; In a) the unoccupied states above the Fermi level have O  $2p$  character and are localized at the neighboring oxygen ions around the vacancy, while in b) they are mainly due to Ti  $3d$  bands of the underlying  $\text{TiO}_2$  layer. [42]

In later experiments [11] it became clear that oxygen vacancies play a significant role at the  $p$ -type interface. We have considered also this more obvious possibility and find that indeed the Fermi level lies in a dip of the DOS both for a vacancy in the  $\text{AlO}_2$  and the SrO-layer [42]. However, states are observed immediately above the Fermi level and these have different character for both cases. In the former (Fig. 8a) they result from the neighboring oxygens around the vacancy, while in the latter (Fig. 8b) they are  $3d$  states of the Ti ion whose apex oxygen is missing. In both cases the vacancies are likely to lead to F-centers.

Park *et al.* [43] have also addressed the electronic behavior at the  $p$ -type as a function of the oxygen vacancy concentration, finding that a system with 25% vacancies in the SrO layer is metallic, while 50% results in a small band gap. We note that the concentration of oxygen vacancies is rather high, but consistent with the 32% estimated from experiment [11].

### 3.3 Thin LAO Films on a STO(001) substrate

Recent experiments on thin LAO films deposited on an STO(001) substrate revealed a significant thickness dependence of the transport properties [51]: The system switches from insulating to conducting behaviour between 3 and 4 monolayers (MLs). Moreover it was shown that metallic behavior can be induced by an external bias even below the critical thickness of 4 MLs and that conducting and insulating regions can be “written” by an atomic force microscope tip [52]. At a first glance these results do not fit in the picture obtained from the DFT calculations for extended LAO/STO superlattices discussed in Section 3.1. In the latter case the compensation mechanism at the  $n$ -type interface is rather local, involving partial occupation of the Ti  $3d$  band independent of the thickness of the LAO or STO layer.

In order to explore the effect of the surface on the interfacial properties we have performed DFT calculations within GGA for 1-5 MLs of LAO on a STO(001) substrate. These are modeled



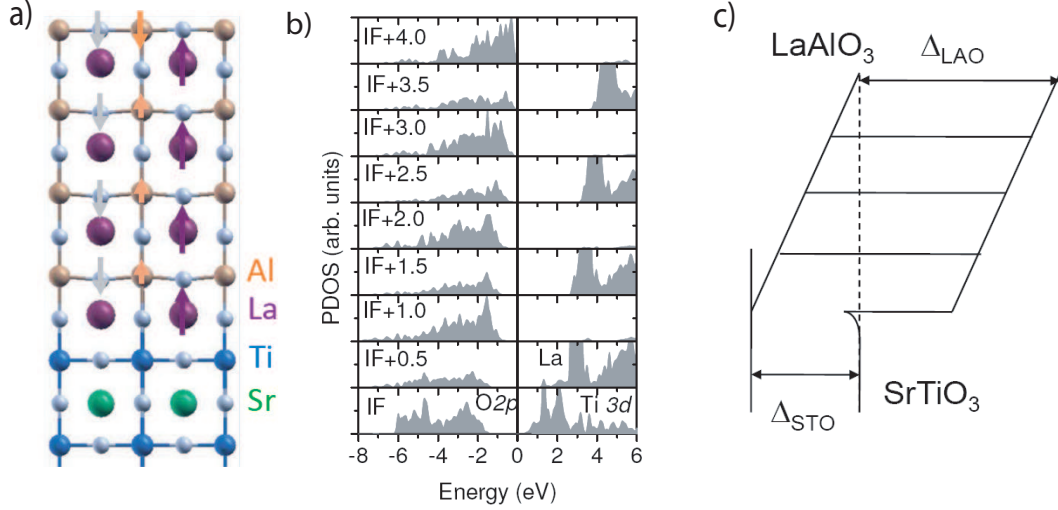


Figure 9: a) Side view of the relaxed structure of 4 MLs LAO/STO(001) showing a strong polar distortion of the LAO film dominated by a 0.2-0.3 Å outward relaxation of La<sup>3+</sup> (purple atoms) and additional buckling in the subsurface AlO<sub>2</sub> layers; b) layer resolved density of states of 4 ML LAO/STO(001) with relaxed positions of the cations. The strong lattice polarization allows the system to remain insulating (here  $E_g = 0.4\text{eV}$ ) until a crossover to an electronic reconstruction takes place at around 5 MLs of LAO/STO(001) [53]. c) schematic figure of the band bending in LAO/STO(001).

in the supercell geometry with two inversion symmetric surfaces on both sides of the slab to avoid spurious electric fields. The surfaces are separated from their periodic images by a vacuum region of  $\sim 10$  Å. In the following we will discuss the role of the lattice relaxations and their implications for the electronic properties.

### 3.3.1 Ionic screening of the electric field

As discussed in the previous Sections, in the LTO/STO and LAO/STO superlattices the ferroelectric distortion is most pronounced in the SrTiO<sub>3</sub> part of the system with a significant buckling of the interface TiO<sub>2</sub> layer. In contrast, for the thin films the strongest ionic displacements are observed in the LaAlO<sub>3</sub> film. In all cases the surface AlO<sub>2</sub> layer relaxes inward with similar values for oxygen and Al, while the subsurface layers show a strong and uniform lattice polarization, dominated by an outward relaxation of La of 0.2-0.3 Å and buckling in the AlO<sub>2</sub> layers. The relaxation pattern for a 4 ML film is shown in Fig. 9a. Using the formal ionic charges we can make a rough estimate of the dipole shift resulting from the polar distortion. We note that these dipole moments include only the ionic part and no contributions due to electron cloud polarization. Indeed, the obtained trend is surprisingly uniform with a layer-resolved dipole moment of  $\sim 0.55$  and  $\sim 0.75$  eÅ in the AlO<sub>2</sub> and LaO layers, respectively and a vanishing dipole moment in the surface AlO<sub>2</sub> and interface TiO<sub>2</sub> layers. Adding these contributions for a 4 ML LAO film on STO(001) results in a total ionic dipole of 4.8 eÅ, which is 60 % and of opposite sign to the bare dipole of the polar LAO film. Thus, the lattice relaxation plays an important role in reducing the electric field generated by the polar LAO-film.

### 3.3.2 Finite Size Effects: Thickness dependent Insulator-to-Metal Transition

The lattice polarization in the LAO film has also a significant impact on the electronic properties: While all systems with bulk positions of the ions show metallic behavior, below the critical thickness the strong lattice polarization allows the system to remain insulating preserving the bulk charge states of the ions. The band gap that opens up upon relaxation of the structure amounts to 1.7 eV for 1 ML LAO/STO(001) but decreases steadily (by  $\sim 0.4$  eV/ML with each added layer). Finally, at a LAO-film thickness of around 5 ML the band gap collapses and a crossover to an electronic reconstruction takes place. In order to gain insight in the underlying mechanisms we have plotted in Fig. 9b the layer-resolved density of states for 4 ML LAO/STO(001). The rigid upward shift of the O2p bands as they approach the surface reflects the strong electric field of the LAO film. In this system, which still has a band gap of 0.4 eV, the valence band maximum is determined by the top of the O2p band in the surface layer, while the conduction band minimum is at the bottom of the Ti 3d states. The electronic reconstruction that emerges beyond 5 MLs of LAO is due to the overlap of these two bands resulting in a finite occupation of the Ti 3d band and some holes in the surface O 2p band. As shown in the schematic picture (Fig. 9c) the potential buildup due to the polar LAO layer causes charge transfer into the narrow band gap STO. This mechanism is intriguing, because it suggests two types of carriers that are spatially separated - holes localized in the surface layer and electrons in the interface layer. Further analysis of the band structure reveals that the band overlap is also indirect in reciprocal space with the bottom of the Ti  $d_{xy}$  band at the  $\Gamma$ -point and the top of the valence O 2p band being at the  $M$ -point. Recent x-ray adsorption spectroscopy measurements have confirmed that the  $d_{xy}$  orbital is the lowest available state for conduction electrons [54]. We note however that the total carrier density just beyond the critical thickness is an order of magnitude lower than the expected  $3.5 \times 10^{14} \text{ cm}^{-2}$  as also found from hard x-ray angle resolved photoelectron spectroscopy [55], but increases continuously with each added layer [56, 57].

The thickness dependent insulator-to-metal transition was also addressed by Ishibashi and Terakura [58] exploiting the recently proposed Coulomb cutoff technique [59] for eliminating any direct Coulomb interaction based coupling between supercells and their periodic images. In their calculations the transition to metallic behavior was obtained already at four overlayers of LAO (the same as experiment) instead of five as in our calculations; this may reflect a  $\sim 0.2$  eV difference in potential rise across the LAO slab, part of which may easily be due to small differences in the atomic relaxations. It is worth mentioning that depending on setup (see discussion in next Section), the choice of exchange correlation potential (LDA vs. GGA), differences in the lateral lattice constant and the resulting atomic relaxations, the calculated critical thickness for the insulator-to-metal transition varies from 3 to 6MLs [52, 53, 58, 60–62]. The predicted critical thickness is likely to be affected also by the band gap underestimation typical for LDA/GGA.

Due to the small occupation of the Ti 3d band after electronic reconstruction sets in, the properties are less influenced by correlation effects compared to the isolated interface. Lee and Demkov [63] have studied 3 and 5 ML LAO on STO(001) using LDA+ $U$  with  $U_{eff} = 8.5$  eV. They find in the latter case a charge transfer exclusively in a split-off Ti state of  $d_{xy}$  character in the interface layer. The pseudo Jahn-Teller effect is discussed as indication of a strong electron-phonon coupling and a possible origin of superconductivity. Breitschaft *et al.* [64] argue that

the shape of scanning tunneling spectroscopy curves is better described using  $U = 2$  eV and that the system shows a two-dimensional electron liquid behavior.

An interesting question is whether holes contribute to the conductivity and whether they can survive in the surface layer or whether other mechanisms - *e.g.* oxygen vacancy formation - can eliminate them. Cen *et al.* [52] have addressed surface vacancies in a 3ML LAO/STO(001) film, showing that when the surface AlO<sub>2</sub> layer is compensated by vacancies, the interface layer becomes metallic with a finite occupation of the Ti 3*d* band. Moreover, the compensation of the surface layer through oxygen vacancies removes also the upward shifts of the oxygen 2*p* bands. Willmott *et al.* addressed the possibility of interdiffusion at the interface by including a LTO layer at the *n*-type interface. [65] This leads also to a metallic state with an enhanced occupation of the Ti 3*d* band at the interface. These results show that the properties at the interface can be affected in important ways by the precise termination, stoichiometry and chemical composition of the surface and interface, thus opening paths to manipulate the electronic behavior of the system.

*Thin LAO films with a p-type interface:* Ishibashi and Terakura [58] found that five layers of LAO over a *p*-type IF remain insulating (recall that five layers over the *n*-type IF is metallic due to band overlap). Thus there is definitely asymmetry for the two types of IFs in this system. They also found that if no atomic relaxation was done (ideal geometries were used), then *every case* was metallic; the electronic system and its screening alone cannot sustain the formal ionic charges in such heterostructures. The analysis of electronic screening in this system, which reveals local response that is virtually impossible to obtain by experiment, initiates an important area of study that needs to be continued and extended to gain fundamental understanding of these heterostructures.

### 3.4 Superlattices with coupled interfaces

As we have seen in the previous Section, deposition of polar LAO films on nonpolar STO(001) results at some point – around four layers in the LAO/STO system – in an electronic reconstruction, which from theoretical studies so far involves a simultaneous electronic reconstruction at the interface and the surface. Experimental probes have not yet established this scenario with certainty.

There is a (somewhat) larger scale version of this issue that merits attention: One can consider the repeated growth of alternating *n*- and *p*-type interfaces [35]. The corresponding supercell has no inversion or mirror symmetry; it is polar and has a dipole. In such a case the *polarization catastrophe* is again an issue, but with an increased distance scale: the repeat distance is the supercell dimension rather than the unit cell dimension. Calculations of such LAO/STO superlattices containing alternating *p* and *n* interfaces have been reported, and they show also thickness dependent phenomena: while LAO<sub>4</sub>/STO<sub>4</sub> superlattices were insulating after structural relaxation [41,43], LAO<sub>*n*</sub>/STO<sub>*n*</sub> beyond *n* = 8 were conducting [66]. Analogous to the thin films, the reconstruction involves electron carriers at the *n*-type interface and hole carriers at the *p*-type interface and transfer between them. These calculations on asymmetric systems/cells raise some conceptual questions about the physical behavior, and also the simulation.

The polar nature of oxides (LAO and LTO in the cases discussed here) led early on to questions about how the experimental heterostructures should be simulated in calculations. To model *isolated* IFs it has been the practice to use (as mentioned above) symmetric supercells, *i.e.* two opposing  $n$ -type IFs in the supercell. Then there is, by symmetry, no dipole in the cell and a periodic, supercell treatment is appropriate. In the study of finite overlayers computational practices have varied. Again, the use of symmetric supercells is straightforward; each half of the cell may have a dipole as determined by the geometry and the (self-consistent) response to electric fields while the opposing dipoles leave a slab that can be treated in a periodic supercell.

This approach makes the cells twice as large and enhances significantly ( $\sim 2^3=8$ ) the computational cost, which is an important practical issue. Finite slabs [60] or repeated opposing  $n$ - and  $p$ -type IFs without inversion symmetry have also been used to model such situations. In such cases the imposition of periodicity on the potential results in an internal electric field in the STO side of the slab that is comparable in magnitude to that in LAO and opposite in sign [66]. Son *et al.* have also modeled asymmetric slabs, [56] employing a “dipole correction” that has been devised [67,68] for finite slabs to correct for the imposed periodicity. The superlattices containing exclusively  $n$ -type interfaces and those with alternating  $n$  and  $p$ -interfaces correspond to two distinct physical situations. Still the question remains as to what extent these can be realized experimentally taking into account possible asymmetry due to roughness and/or defects. The comparison of various methods and comparison with experiment needs further consideration to obtain a reliable physical picture.

## 4 Modeling Oxide Interfaces: Summary and Perspectives for the Future

In summary, first principles calculations suggest that at an interface between a polar and a nonpolar material different compensation mechanisms may be at work, depending on some rather detailed features. For infinitely extended superlattices of the Mott insulator LTO and the band insulator STO and in superlattices containing  $n$ -type LAO/STO interfaces, the ground state is a charge and orbitally ordered  $\text{Ti}^{3+}$ ,  $\text{Ti}^{4+}$ -layer with an occupied  $d_{xy}$  orbital at the  $\text{Ti}^{3+}$  sites. Structural relaxation within GGA+ $U$  including a larger lateral periodicity leads to a further confinement of the excess electron at the interface. On the other hand, relaxation within GGA within a  $p(1 \times 1)$  lateral unit cell leads to a delocalization and redistribution of the charge throughout the STO part of the superlattice (overscreening), significantly increasing the confinement length of the electron gas. This scenario is likely to happen at higher temperatures when electron hopping is possible.

In contrast, a completely different situation arises in thin LAO films on a STO(001) substrate. Here a strong and uniform lattice polarization leads to an insulating behavior for a few LAO layers. However, the potential buildup with each added LAO layer invokes a reduction of the band gap and finally an insulator-to-metal transition and an electronic reconstruction but with a much lower carrier density than expected from formal electron counting. We note that the finite size effects are not restricted to LAO films on STO but has also been reported experimentally for *e.g.* LVO/STO(001) [70, 71].

Recent measurements of Hwang et al. [69] show that thin LAO films (5-10 MLs) exhibit metallic temperature dependence, while thicker films (up to 25 MLs) show an upturn of the sheet resistance at low temperatures. These findings seem to support the DFT results suggesting a coupling of surface and interface in the thinner films and an interface confined compensation mechanism at more isolated interfaces possibly connected with localization and charge ordering.

The electronic behavior in thin LAO is likely to be very sensitive to defects and adsorbates. DFT calculations [52] give indications that oxygen vacancies can cancel the potential buildup observed in shifts of the O  $2p$  bands in the non-defective films. Moreover, adsorbates or a nonpolar oxide layer [72] can modify significantly the properties of the system. Thus, finite size effects (film thickness) together with a number of further parameters (e.g. defects, adsorbates, an oxide overlayer or an external bias) can be used to tailor the interfacial properties and need further attention in future.

In this review we have concentrated on systems where the charge mismatch is due to a  $d^1-d^0$  occupation across the interface, and we have seen that electronic correlations can lead to novel compensation mechanisms unanticipated from semiconductor heterostructures. These processes open the possibility of realizing novel charge, orbital and magnetically ordered states. A further degree of complexity arises when both transition metal ions across the interface contain  $d$  electrons and e.g. the valence mismatch across the interface is enhanced. The competition between these ions to compensate the charge mismatch at the interface may result in complex orbital physics and promises to lead to a plethora of new electronic phases. Obtaining a fundamental understanding of the phenomena that arise at polar transition metal oxide interfaces could lead to novel concepts for oxide-based electronics devices.

While we have considered here oxide heterostructures with perovskite structure, analogous effects can arise also in other systems. An example for a polar interface where the constituents have a corundum derived structure is the hematite-ilmenite system. A stacking of  $2\text{Fe}^{3+}/3\text{O}^{2-}$  layers in hematite and  $2\text{Fe}^{2+}/3\text{O}^{2-}/\text{Ti}^{4+}$  in ilmenite results in a polar discontinuity across the  $\text{Fe}_2\text{O}_3$ - $\text{FeTiO}_3$ -interface. DFT calculations including an on-site Coulomb correction [73,74] give theoretical evidence for the lamellar magnetism hypothesis [75]: a mixed  $\text{Fe}^{2+}$ ,  $\text{Fe}^{3+}$  contact layer is formed to accommodate the charge mismatch. The uncompensated moments in the interface layer give rise to ferrimagnetism at the interface between the canted antiferromagnet  $\text{Fe}_2\text{O}_3$  and the room-temperature paramagnet  $\text{FeTiO}_3$ . This interface induced magnetism makes this system interesting e.g. for spintronics applications.

Unanticipated phenomena can arise also in heterostructures without a polar discontinuity. For example the confinement of the electrons in a heterostructure and lattice strain have been suggested as a means to control the orbital occupation [76]. So far much of the focus has been on “conducting versus insulating” behavior. However, a recent discovery has illustrated that such a question does not cover all possibilities. Calculations on  $\text{VO}_2/\text{TiO}_2$  heterostructures, non-polar and seemingly having only the  $d^1-d^0$  aspect to arouse interest, display a previously unknown electronic structure, consisting of point Fermi surfaces as does graphene, but possessing a highly anisotropic behavior: in the 2D plane the electrons have nearly free character, but in the perpendicular direction the dispersion is massless, like the dispersion (in both directions) in graphene. These “semi-Dirac” points so far exist only in two-dimensional oxide heterostructures, and their



study may rival the activity in graphene. The low energy behavior is distinct [78] not only from graphene but also from another point Fermi surface system, the zero-gap semiconductor. The very different physical structure compared to graphene (robust heterostructure versus a flexible monatomic sheet) will likely lead to very different applications. Fundamental understanding of both polar effects, and the characteristics of dispersion, should be important aspects of future studies.

Finally, another complexity should be noted. In the studies of polar interfaces, correlation effects arising from strong intra-atomic interaction have been shown to lead to very different behavior than arises if such effects are neglected. However, so far such interactions have been treated (nearly always) in a static, mean-field manner. It is one of the fundamental precepts of strongly correlated systems that upon doping (which is very likely to occur at some level, perhaps inadvertently) dynamical processes come into play and determine many of the properties of doped correlated insulators. Including such dynamical effects, and especially doing so self-consistently, will be an important part of the next generation of theoretical modeling of oxide heterostructures.

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